Question Number : 1
Correct : 1 Wrong : 0

If
\[
\int_0^\pi \int_0^\pi \frac{\sin y}{y} \, dy \, dx = \frac{1}{2}
\]
for some \( \alpha \geq 1 \), then the value of \( \alpha \) is ________.

Question Number : 2
Correct : 1 Wrong : -0.33

Three fair dice are rolled simultaneously. The probability of getting a sum of 5 is

(A) \( \frac{1}{108} \)  (B) \( \frac{1}{72} \)  (C) \( \frac{1}{54} \)  (D) \( \frac{1}{36} \)

Question Number : 3
Correct : 1 Wrong : 0

Suppose \( \alpha, \beta, \gamma \) and \( \delta \) are constants such that
\[
p(x) = \delta + \gamma (x + 1) + \beta x(x + 1) + \alpha x(x + 1)(x - 1)
\]
is the interpolating polynomial for the data \((-1, -3), (0,1), (1, -1), \) and \((2, -3)\). Then the value of \( \gamma - \beta \) is ________.

Question Number : 4
Correct : 1 Wrong : 0

Consider the ordinary differential equation
\[
y'' + \alpha y' + \beta y = 0,
\]
where \( \alpha \) and \( \beta \) are constants. If \( y(x) = x e^x \) is a solution of the above equation, then the value of \( \beta - \alpha \) is ________.

Question Number : 5
Correct : 1 Wrong : -0.33

Consider the system of linear equations
\[
2x_2 + x_3 = 0, \\
-2x_1 - x_3 = 0, \\
-x_1 + x_2 = 1.
\]

The above system has
(A) a unique solution
(B) infinite number of solutions
(C) no solution
(D) only two distinct solutions
Let $C$ be a simple smooth closed curve enclosing the region $R$ in the $xy$-plane. Let $C$ be oriented counterclockwise. If the value of the integral
\[ \int_C \left( y + e^{x^2} \right) dx + \left( 3x + \cos y \right) dy \]
is 16, then the area of $R$ is ________.

**Question Number : 7**

Consider the ordinary differential equation
\[ x^2y'' + xy' - y = x, \quad x > 0. \]
In terms of arbitrary constants $c_1$ and $c_2$, the general solution of the above equation is

(A) $y(x) = c_1x + c_2x^{-1} + x^3$
(B) $y(x) = c_1x^2 + c_2x^{-1} + \frac{1}{2}x$
(C) $y(x) = c_1x + c_2x^{-1} + \frac{1}{2}x \ln x$
(D) $y(x) = c_1x + c_2 + x^{-1}$

**Question Number : 8**

Let $f: \mathbb{R} \to \mathbb{R}$ and $g: \mathbb{R} \to \mathbb{R}$ be defined by
\[ f(x) = \begin{cases} x \left( \sin x \right) \cos \frac{1}{x}, & x \neq 0 \\ 0, & x = 0 \end{cases} \quad \text{and} \quad g(x) = \begin{cases} x \cos \frac{1}{x}, & x \neq 0 \\ 0, & x = 0 \end{cases}, \]
where $\mathbb{R}$ denotes the set of real numbers. Then, at $x = 0$,

(A) $f$ is differentiable but $g$ is NOT differentiable
(B) $f$ is NOT differentiable but $g$ is differentiable
(C) both $f$ and $g$ are differentiable
(D) neither $f$ nor $g$ is differentiable
If \( u(x, t) = g(t) \sin x \) is the solution of the wave equation
\[ u_{tt} = u_{xx}, \quad t > 0, \quad 0 < x < \pi, \]
with the initial conditions
\[ u(x, 0) = 2 \sin x, \quad u_t(x, 0) = 0, \quad 0 \leq x \leq \pi, \]
and the boundary conditions
\[ u(0, t) = u(\pi, t) = 0, \quad t \geq 0, \]
then the value of \( g\left(\frac{\pi}{3}\right) \) is \underline{__________}.

Question Number : 10
Correct : 2  Wrong : 0

Let
\[ I = \int_0^1 \frac{1}{1 + t} \, dt + \frac{\pi i}{2} \int_0^1 \frac{e^{\frac{2\pi i t}{\ln t}}}{1 + e^{\frac{2\pi i}{\ln t}}} \, dt - i \int_0^1 \frac{1}{1 + it} \, dt, \]
where \( t \) is a real variable and \( i = \sqrt{-1} \). The value of \( I \) is \underline{__________}.

Question Number : 11
Correct : 2  Wrong : -0.66

Let
\[ a_k = 2^{-k} k^4 \sin k \quad \text{and} \quad b_k = 2^{-k^2} k \sin^2 k \]
for \( k = 1, 2, \ldots \). Then

(A) \( \sum_{k=1}^\infty a_k \) converges but \( \sum_{k=1}^\infty b_k \) does NOT converge
(B) \( \sum_{k=1}^\infty a_k \) does NOT converge but \( \sum_{k=1}^\infty b_k \) converges
(C) both \( \sum_{k=1}^\infty a_k \) and \( \sum_{k=1}^\infty b_k \) converge
(D) neither \( \sum_{k=1}^\infty a_k \) nor \( \sum_{k=1}^\infty b_k \) converges
Question Number : 165
Correct : 2  Wrong : -0.66

Which among the following statement(s) is (are) correct.

P: ENSO and El-Nino are the same and refer to the warming of Equatorial Eastern Pacific SST.
Q: ENSO is an atmosphere-ocean coupled phenomenon and El-Nino is its oceanic part.
R: ENSO is an atmospheric phenomenon and El-Nino is an oceanic phenomenon
S: ENSO is the oscillatory component of El-Nino having a period of 4.7 years.

(A) P & R  (B) Only Q  (C) P, Q and S  (D) R & S

General Aptitude

Question Number : 166
Correct : 1  Wrong : -0.33

The event would have been successful if you ____________ able to come.

(A) are  (B) had been  (C) have been  (D) would have been

Question Number : 167
Correct : 1  Wrong : -0.33

There was no doubt that their work was thorough.

Which of the words below is closest in meaning to the underlined word above?

(A) pretty  (B) complete  (C) sloppy  (D) haphazard
Question Number: 168  Correct: 1  Wrong: -0.33

Four cards lie on a table. Each card has a number printed on one side and a colour on the other. The faces visible on the cards are 2, 3, red, and blue.

Proposition: If a card has an even value on one side, then its opposite face is red.

The cards which MUST be turned over to verify the above proposition are

(A) 2, red  (B) 2, 3, red  (C) 2, blue  (D) 2, red, blue

Question Number: 169  Correct: 1  Wrong: -0.33

What is the value of \( x \) when \( 81 \times \left(\frac{16}{25}\right)^{x+2} \div \left(\frac{3}{5}\right)^{2x+4} = 144 \)?

(A) 1  (B) -1  (C) -2  (D) Cannot be determined

Question Number: 170  Correct: 1  Wrong: -0.33

Two dice are thrown simultaneously. The probability that the product of the numbers appearing on the top faces of the dice is a perfect square is

(A) 1/9  (B) 2/9  (C) 1/3  (D) 4/9

Question Number: 171  Correct: 2  Wrong: -0.66

Bhaichung was observing the pattern of people entering and leaving a car service centre. There was a single window where customers were being served. He saw that people inevitably came out of the centre in the order that they went in. However, the time they spent inside seemed to vary a lot: some people came out in a matter of minutes while for others it took much longer.

From this, what can one conclude?

(A) The centre operates on a first-come-first-served basis, but with variable service times, depending on specific customer needs.
(B) Customers were served in an arbitrary order, since they took varying amounts of time for service completion in the centre.
(C) Since some people came out within a few minutes of entering the centre, the system is likely to operate on a last-come-first-served basis.
(D) Entering the centre early ensured that one would have shorter service times and most people attempted to do this.
A map shows the elevations of Darjeeling, Gangtok, Kalimpong, Pelling, and Siliguri. Kalimpong is at a lower elevation than Gangtok. Pelling is at a lower elevation than Gangtok. Pelling is at a higher elevation than Siliguri. Darjeeling is at a higher elevation than Gangtok.

Which of the following statements can be inferred from the paragraph above?

i. Pelling is at a higher elevation than Kalimpong
ii. Kalimpong is at a lower elevation than Darjeeling
iii. Kalimpong is at a higher elevation than Siliguri
iv. Siliguri is at a lower elevation than Gangtok

(A) Only ii  (B) Only ii and iii  (C) Only ii and iv  (D) Only iii and iv

Question Number : 173

P, Q, R, S, T and U are seated around a circular table. R is seated two places to the right of Q. P is seated three places to the left of R. S is seated opposite U. If P and U now switch seats, which of the following must necessarily be true?

(A) P is immediately to the right of R
(B) T is immediately to the left of P
(C) T is immediately to the left of P or P is immediately to the right of Q
(D) U is immediately to the right of R or P is immediately to the left of T

Question Number : 174

Budhan covers a distance of 19 km in 2 hours by cycling one fourth of the time and walking the rest. The next day he cycles (at the same speed as before) for half the time and walks the rest (at the same speed as before) and covers 26 km in 2 hours. The speed in km/h at which Budhan walks is

(A) 1  (B) 4  (C) 5  (D) 6
The points in the graph below represent the halts of a lift for durations of 1 minute, over a period of 1 hour.

Which of the following statements are correct?

i. The elevator never moves directly from any non-ground floor to another non-ground floor over the one hour period

ii. The elevator stays on the fourth floor for the longest duration over the one hour period

(A) Only i  (B) Only ii  (C) Both i and ii  (D) Neither i nor ii